5. Data presentation

"Above all else show the data"

Edward R. Tufte

A good plot

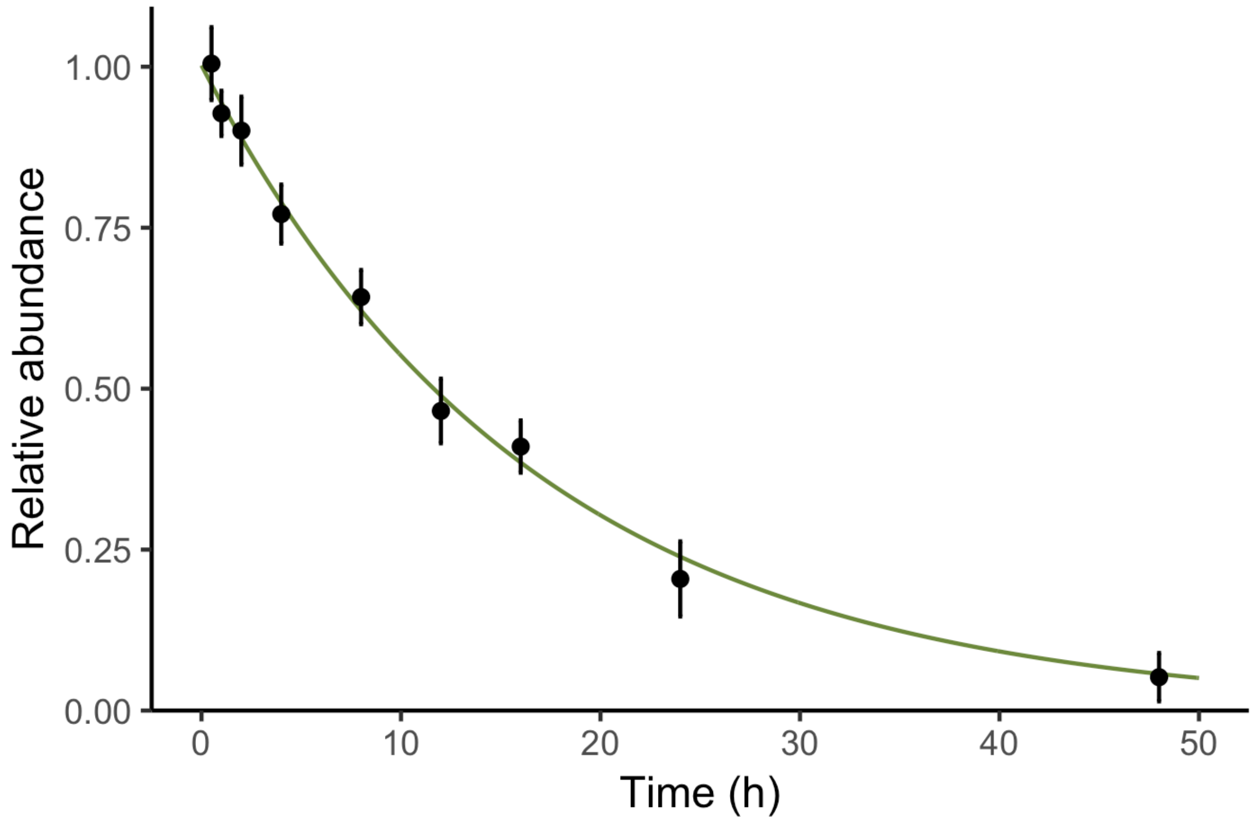


Figure 6-1. Exponential decay of a protein in a simulated experiment. Error bars represent standard errors. The curve shows the best-fitting exponential decay model, $y(t) = Ae^{-t/\tau}$, with $A = 1.00 \pm 0.03$ and $\tau = 17 \pm 1$ h (95% confidence intervals).

3 rules for making good plots

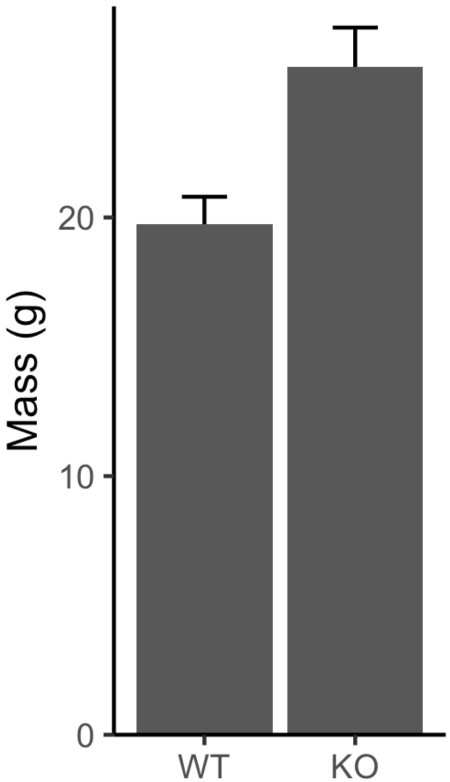
1. Clarity of presentation

2. Clarity of presentation

3. Clarity of presentation

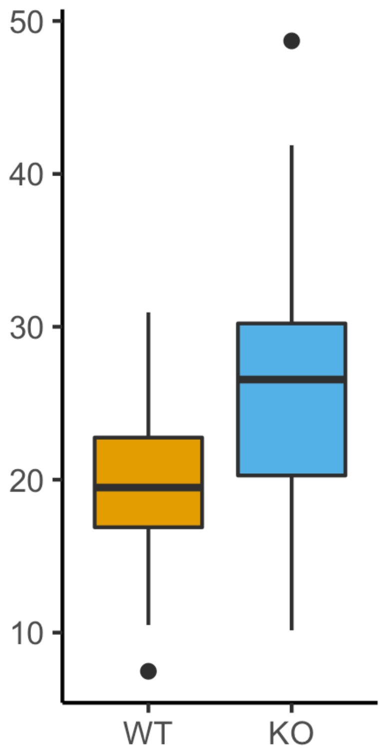
Show your data!

Awful!



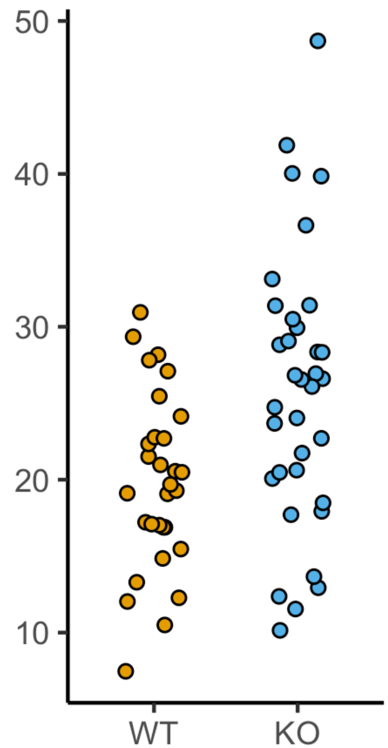
Dynamite plot

OK



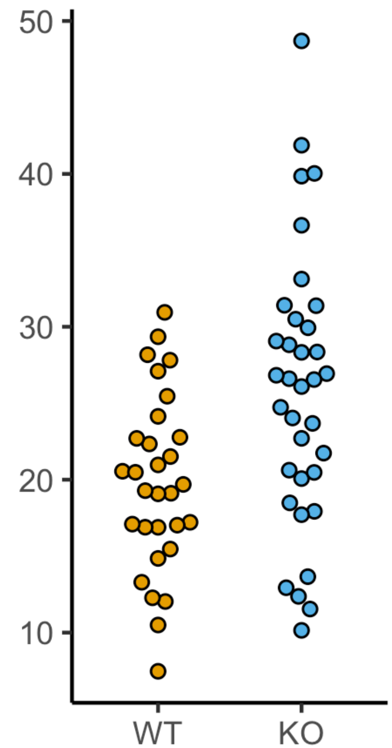
Box plot

Better



Jitter plot

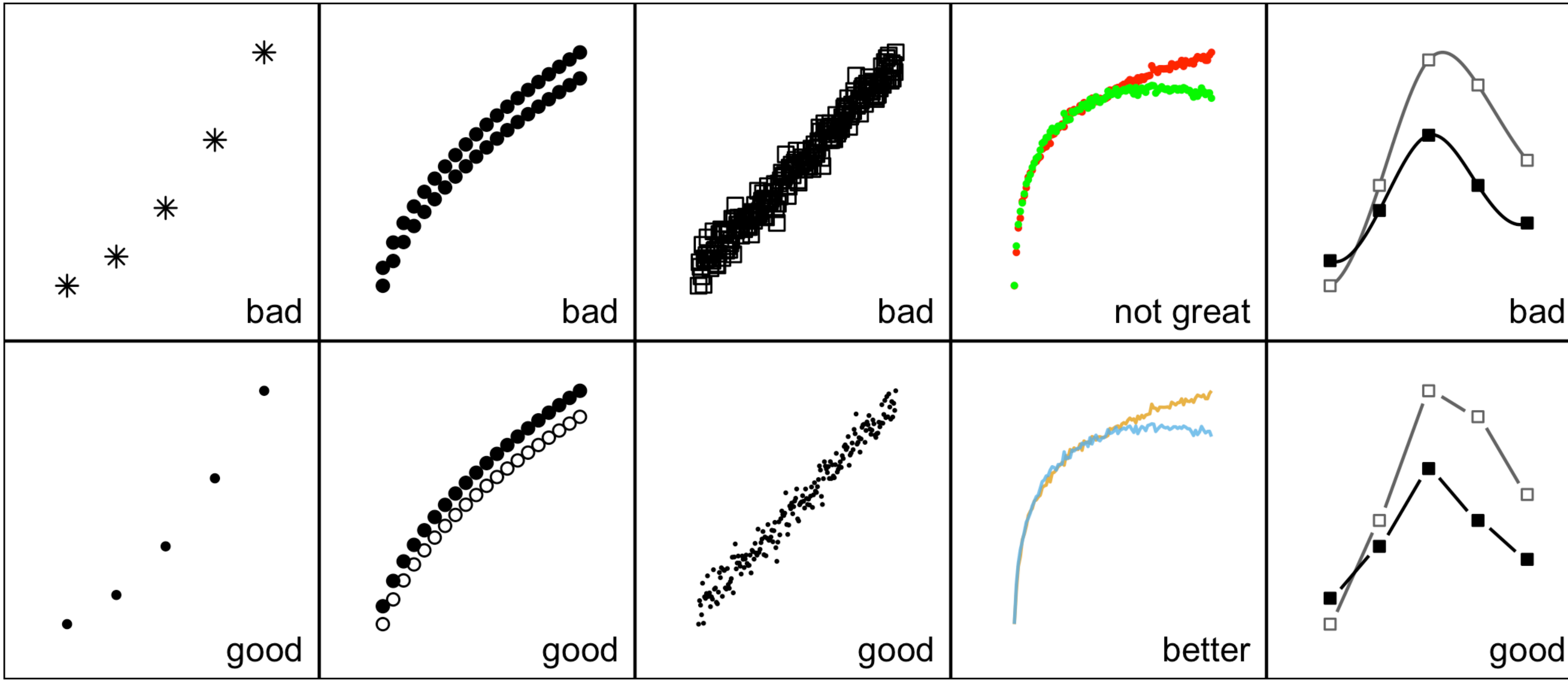
Best!



Beeswarm plot

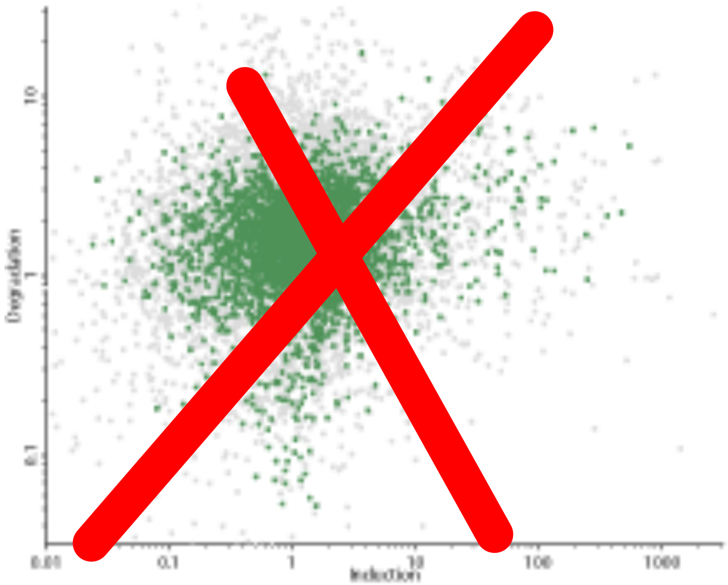
```
library(ggplot2)
library(ggbeeswarm)
library(dplyr)

set.seed(1001)
n1 <- 30
n2 <- 35
d <- data.frame(
  type = c(rep("WT", n1), rep("KO", n2)),
  value = c(rnorm(n1, 20, 5), rnorm(n2, 25, 7))
)
d$type <- relevel(d$type, ref="WT")

dm <- d %>% group_by(type) %>% summarise(M = mean(value), SE = sd(value) / sqrt(n()))

g0 <- ggplot() +
  theme_classic() + theme(legend.position = "none") +
  scale_fill_manual(values=c("#E69F00", "#56B4E9")) + labs(x=NULL, y=NULL)

g0 +
  geom_errorbar(data=dm, aes(x=type, ymin=M-SE, ymax=M+SE), width=0.3, colour="black") +
  geom_col(data=dm, aes(x=type, y=M)) +
  scale_y_continuous(expand=c(0,0), limits=c(0, max(dm$M + dm$SE) * 1.03 )) +
  labs(y="Mass (g)")

g0 +
  geom_boxplot(data=d, aes(x=type, y=value, fill=type))

g0 +
  geom_jitter(data=d, aes(x=type, y=value, fill=type), shape=21, width=0.2, height=0)

g0 +
  geom_beeswarm(data=d, aes(x=type, y=value, fill=type), shape=21, cex=4.5)
```

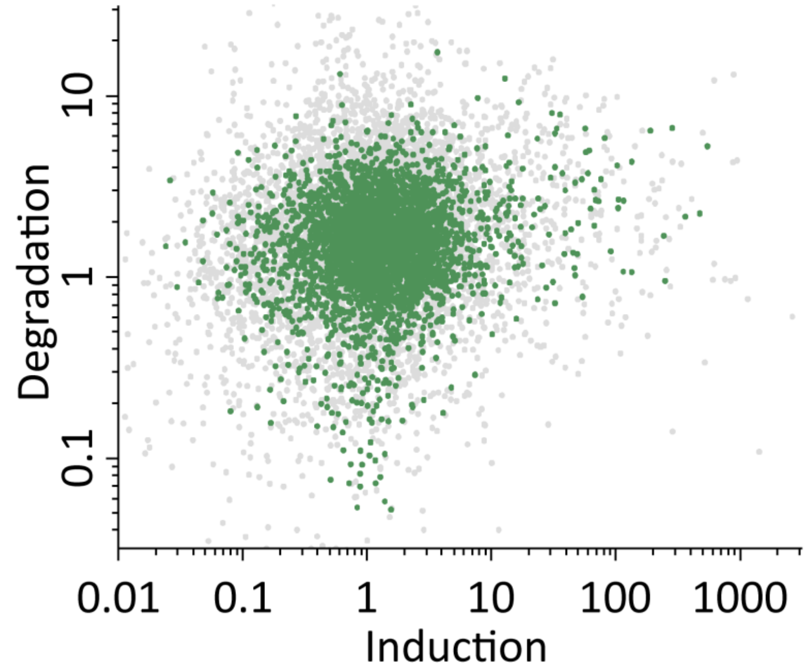
Lines and symbols



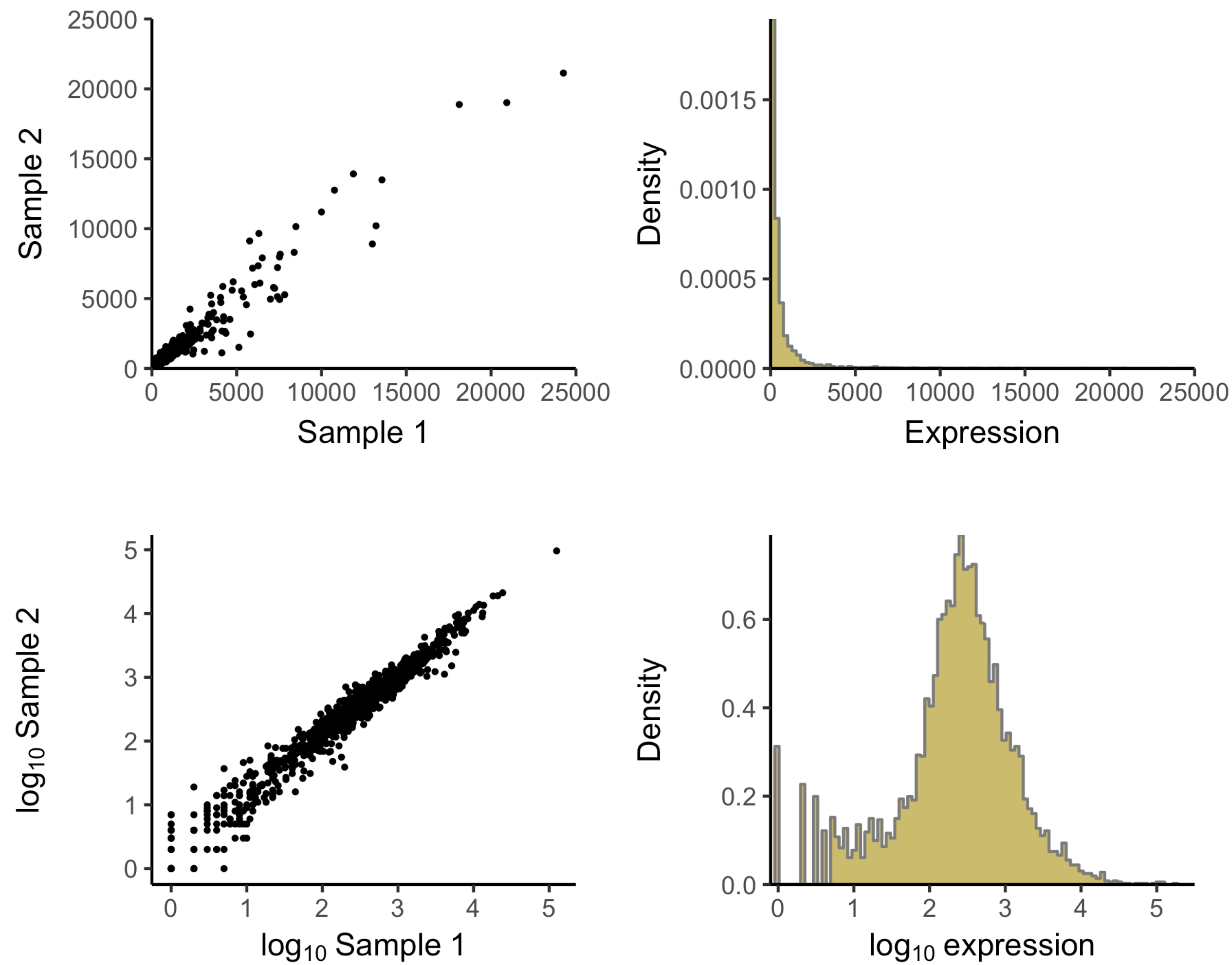
- Clarity!
- Symbols shall be easy to distinguish
- It is OK to join data points with lines for guidance

Labels!

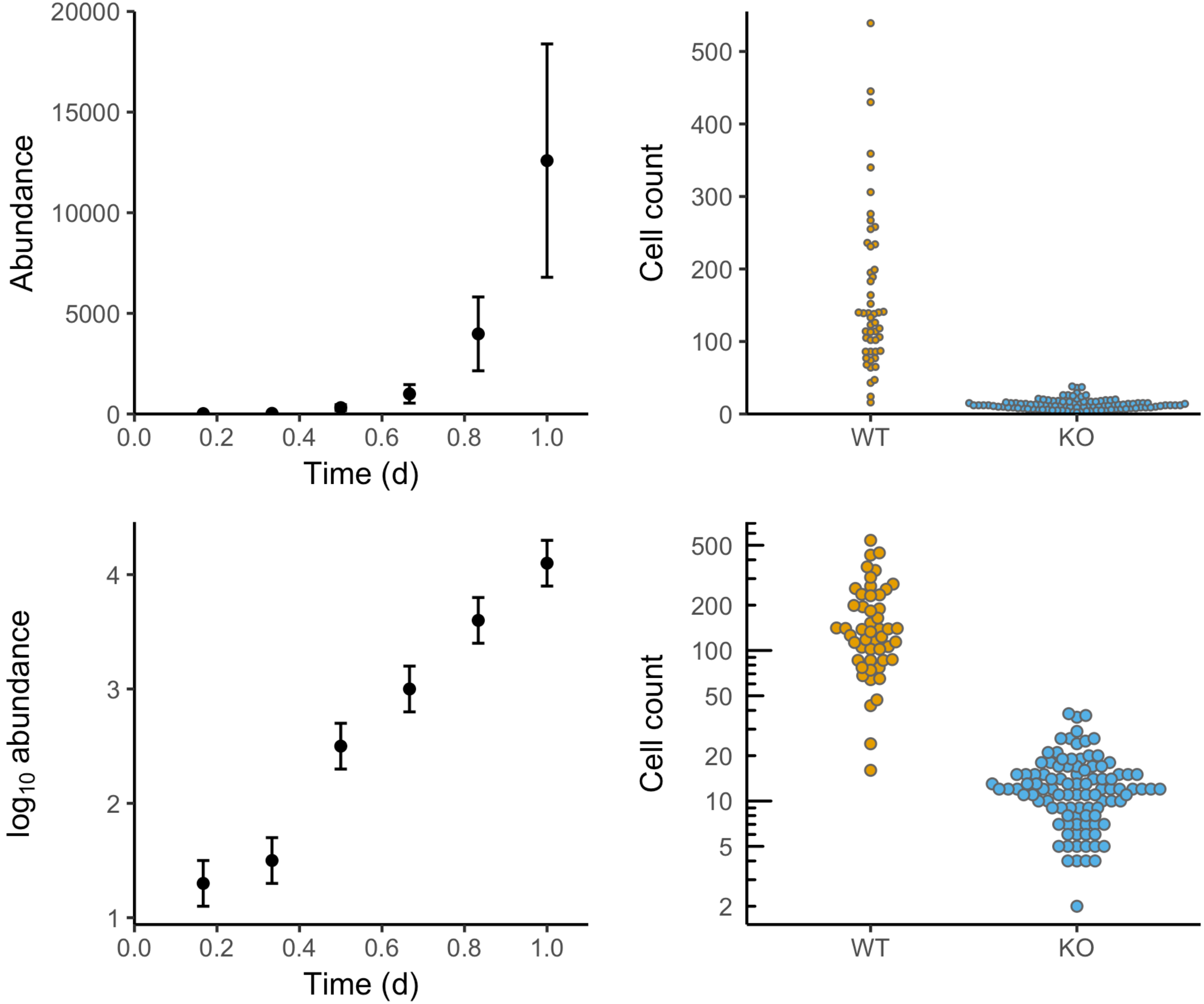




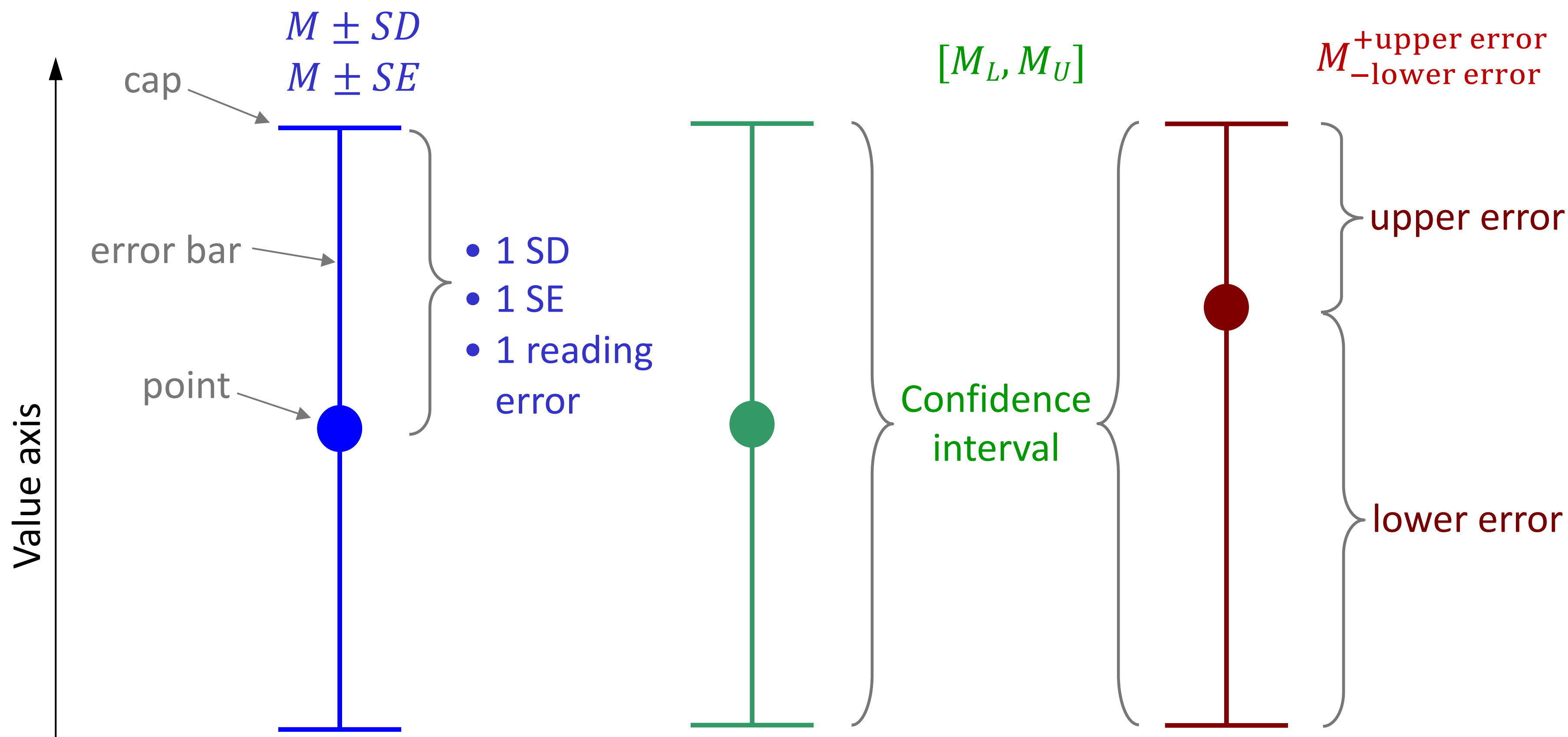
Logarithmic plots



Logarithmic plots



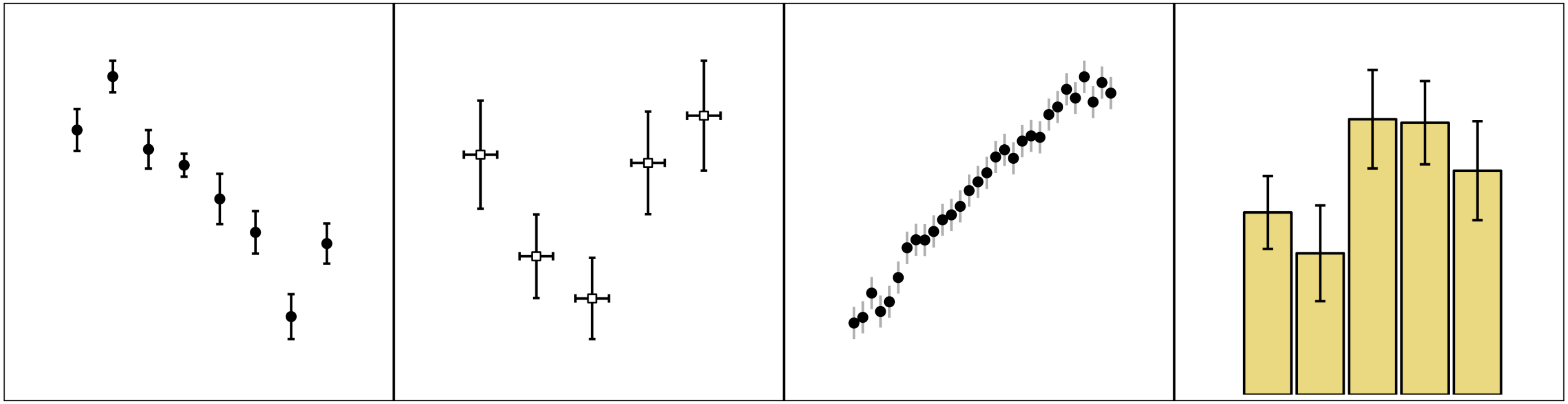
How to plot error bars



The point represents

- statistical estimator (e.g. sample mean)
- best-fitting value
- direct measurement

How to plot error bars



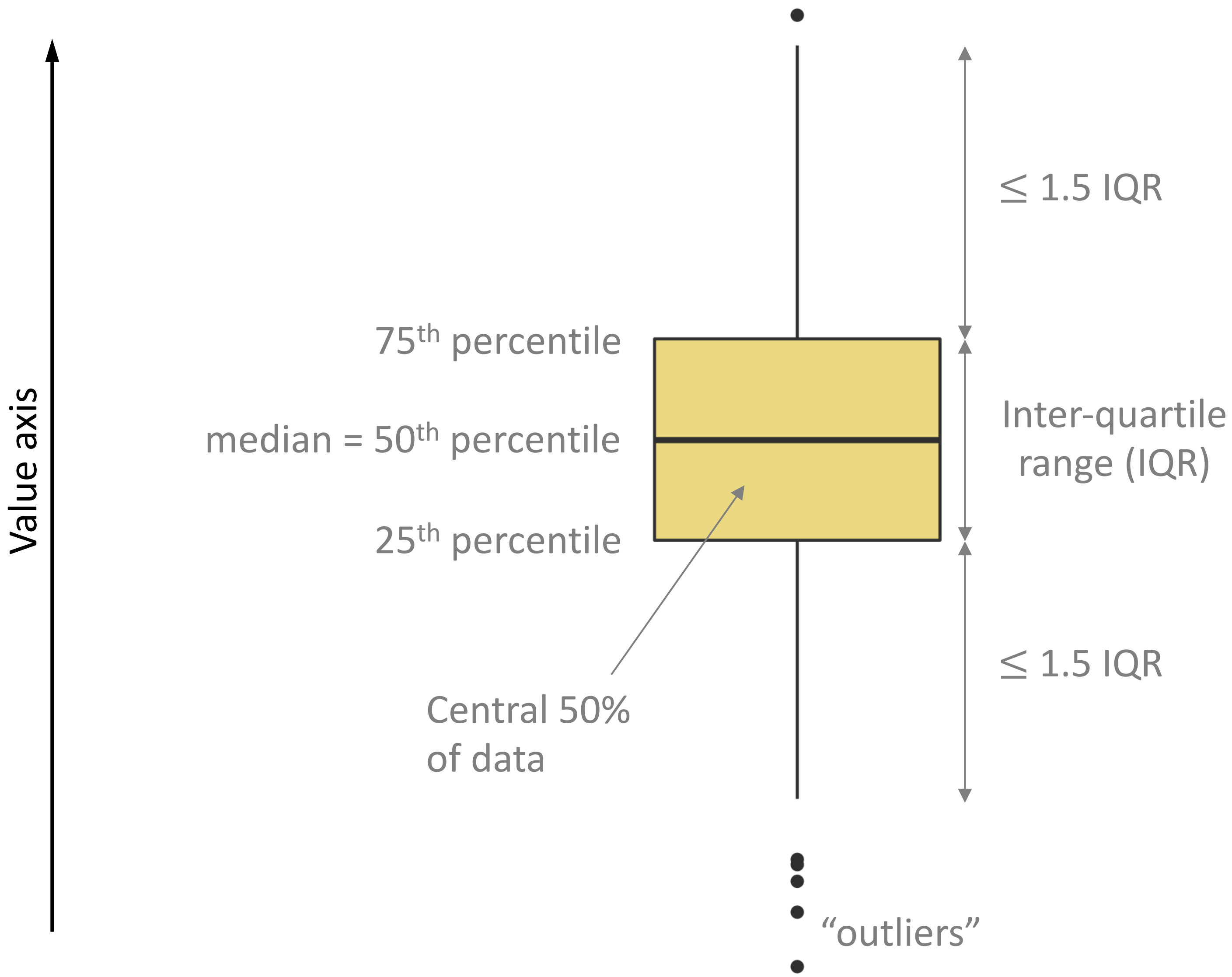
- Clarity!
- Make sure error bars are visible

Types of errors

Error bar	What it represents	When to use
Standard deviation	Scatter in the sample	Comparing two or more samples, though box plots (with data points) make a good alternative
Standard error	Error of the mean	Most commonly used error bar, though confidence intervals have better statistical intuition
Confidence interval	Confidence in the result	The best representation of uncertainty; can be used in almost any case

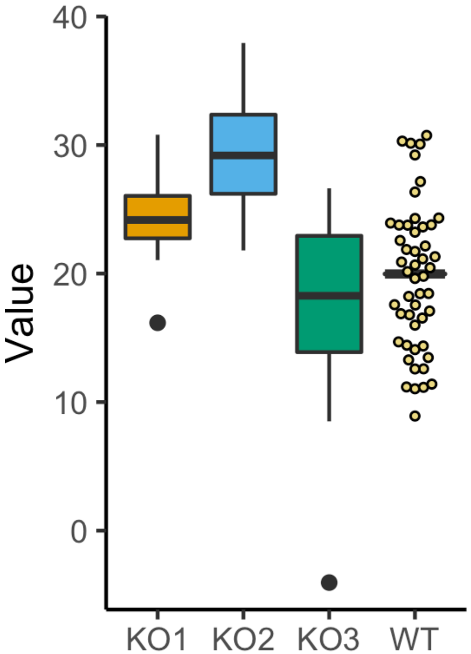
- Always state what type of uncertainty is represented by your error bars

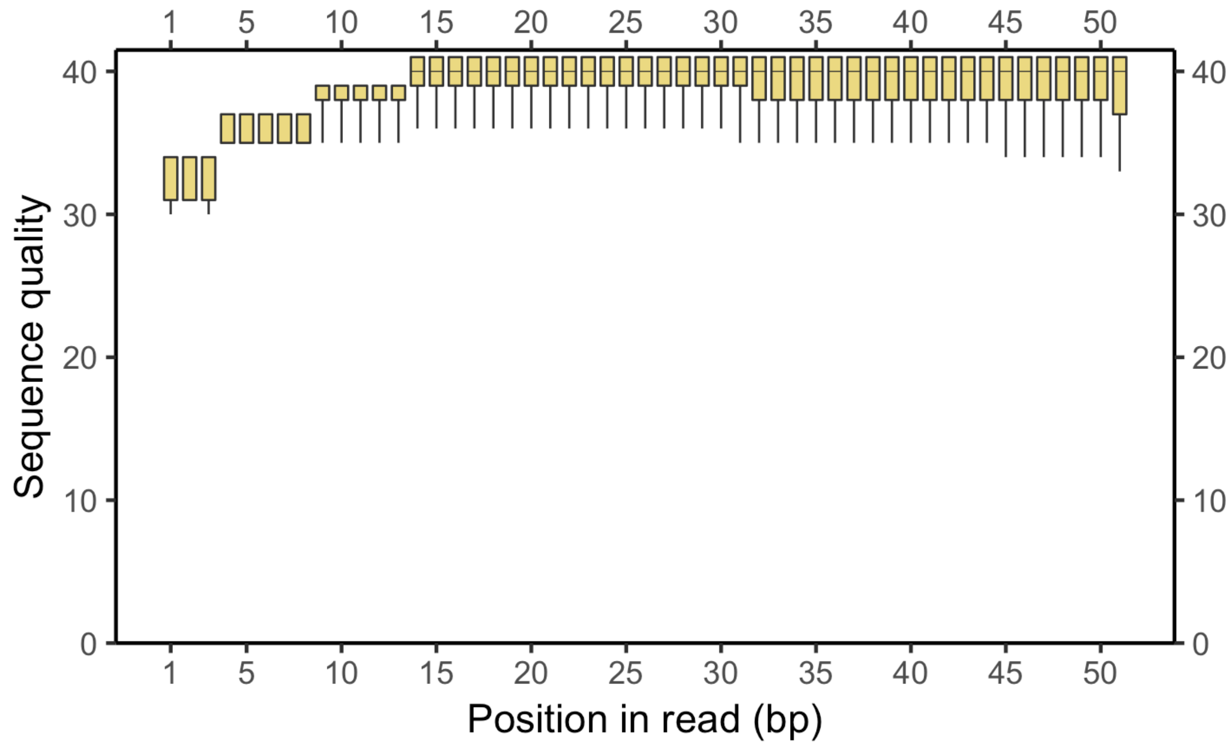
Box plots



Value axis
75th percentile
median = 50th percentile
25th percentile
Central 50% of data
≤ 1.5 IQR
Inter-quartile range (IQR)
≤ 1.5 IQR
"outliers"

Box plots



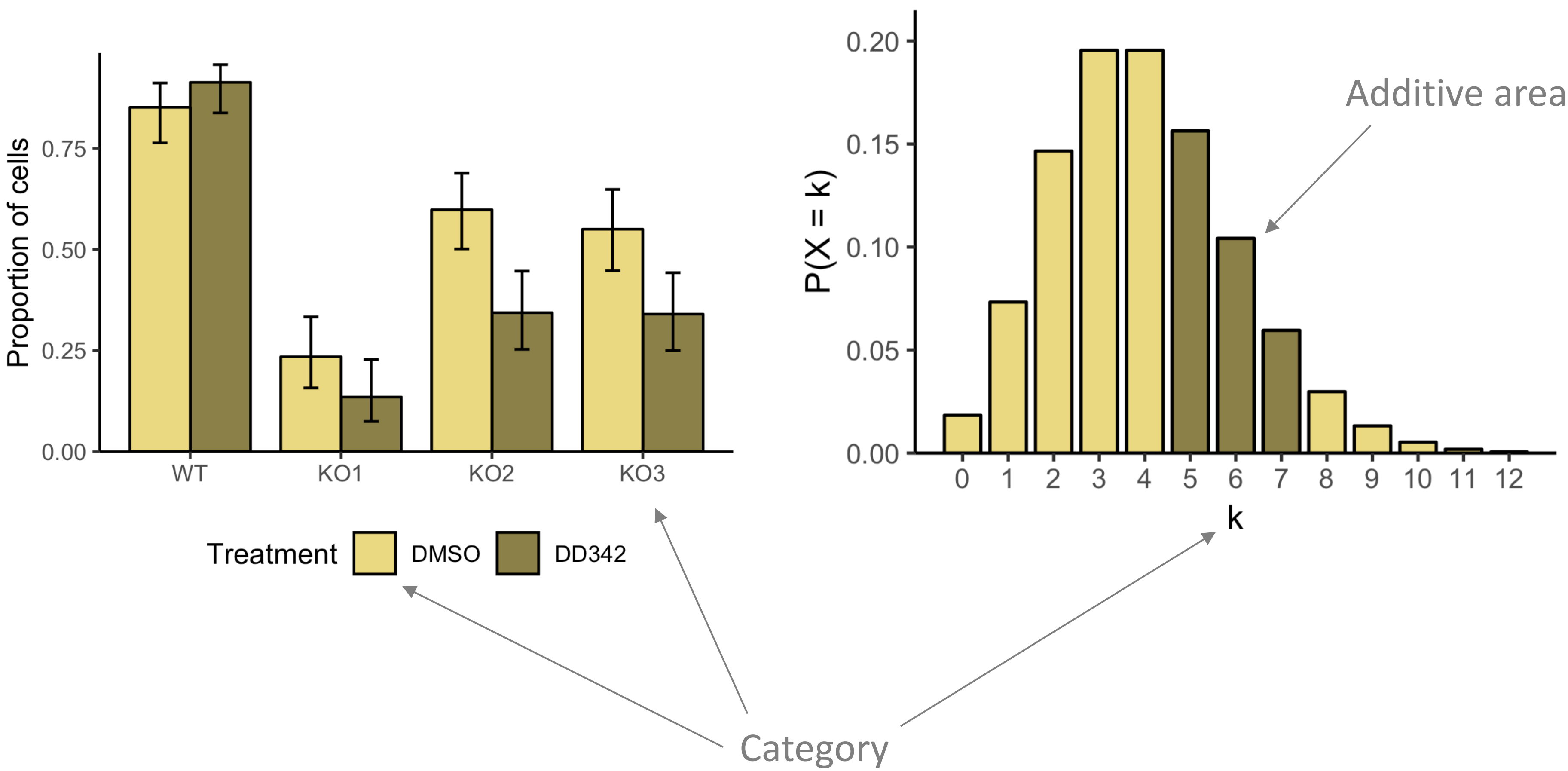


- Box plots are a good alternative to standard deviation error bars
- They are non-parametric and show pure data
- Useful for large number of data points

Bar plots: categorical variable

Proportion or count

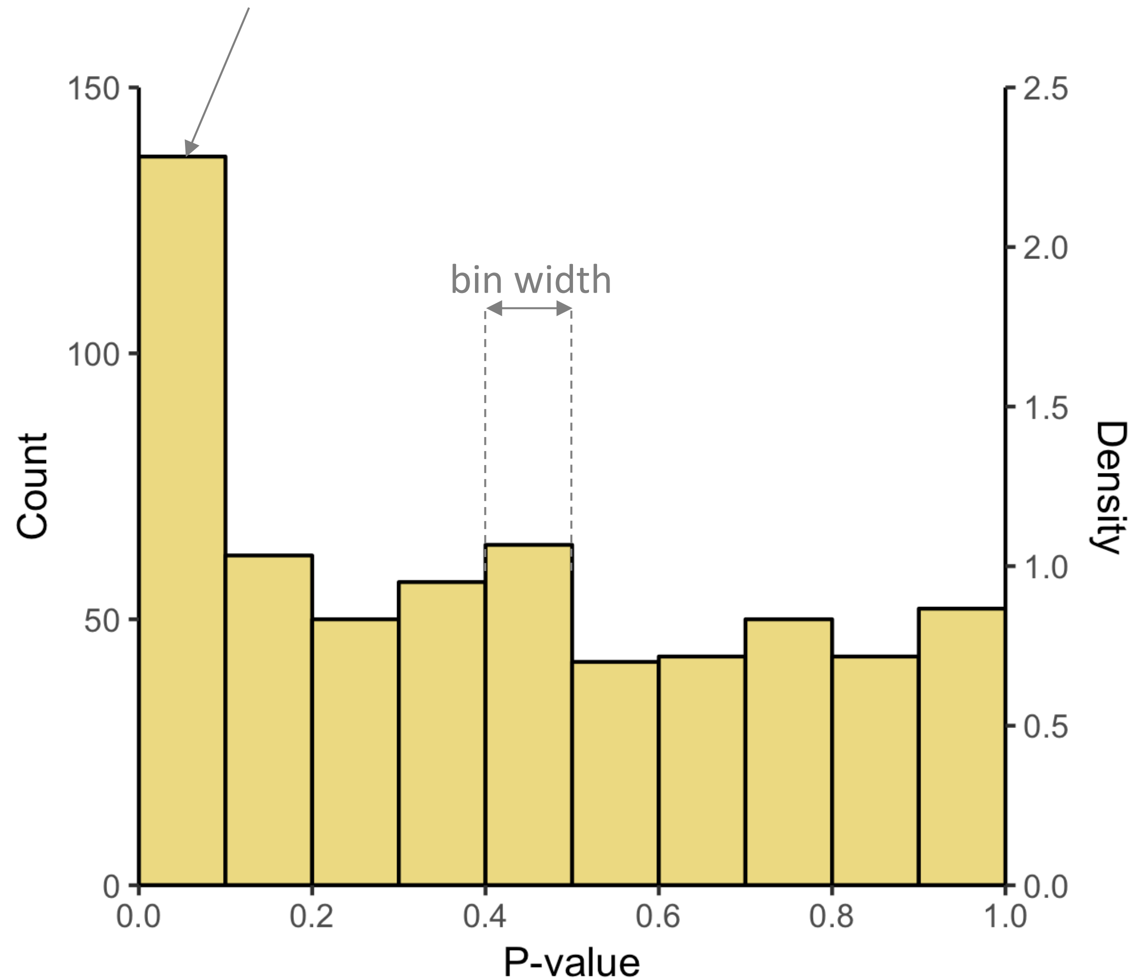
Probability distribution



Bar plots: continuous variable

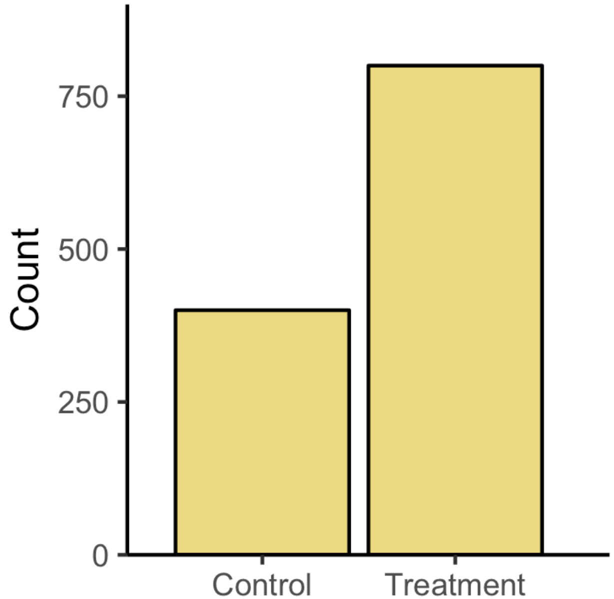
count = 137
density = 2.28

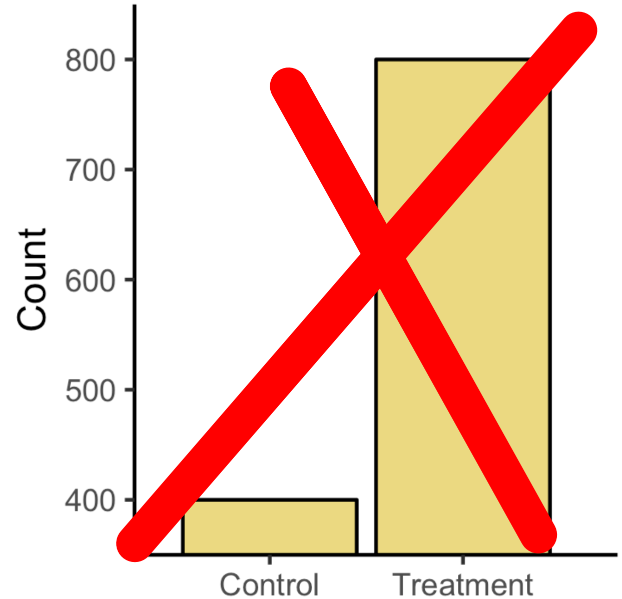
$$\text{density} = \frac{\text{count}}{\text{total count} * \text{bin width}}$$



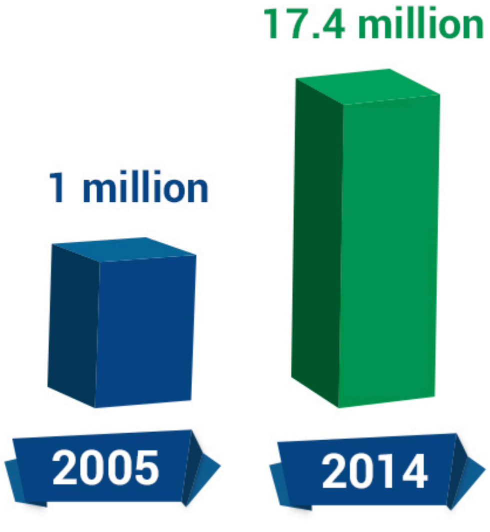
Total area = 1

Bar plots start at zero

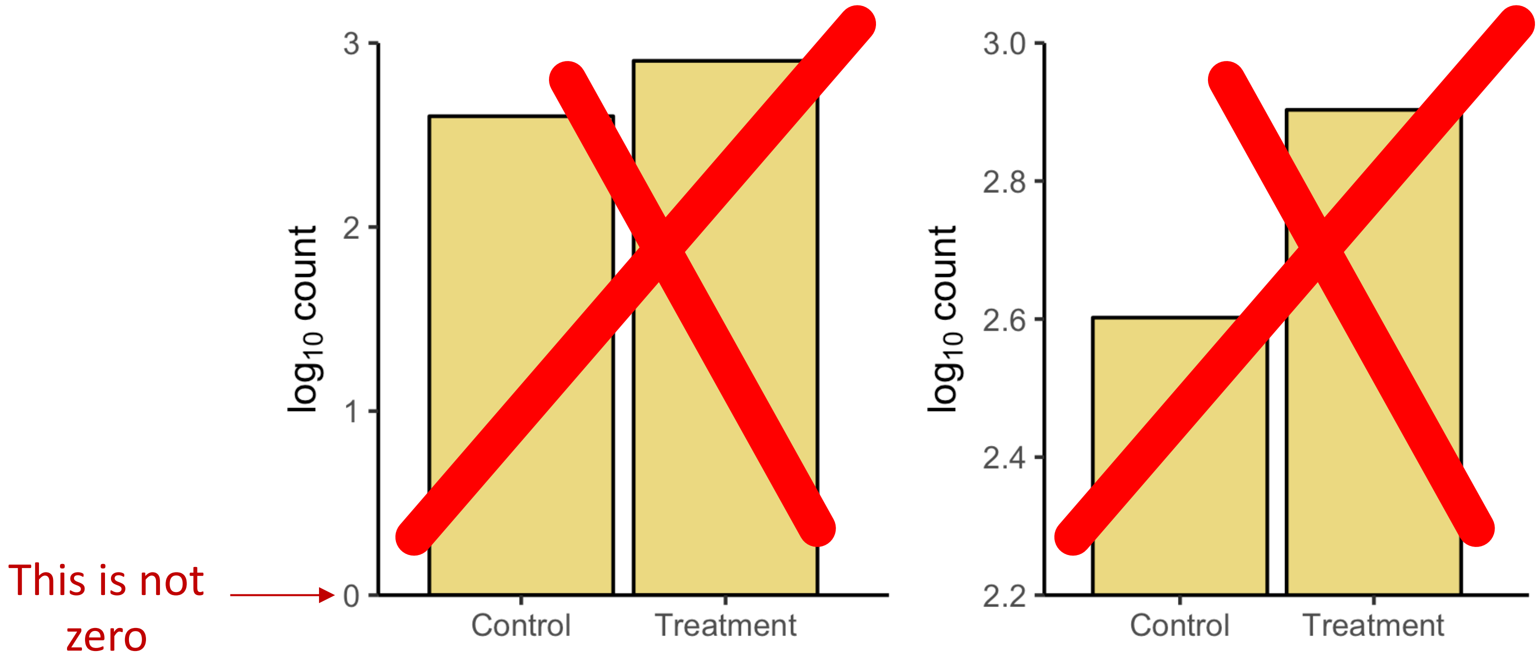




- Bar area represents its value
- Hence, baseline must be at zero!



Bar plots in logarithmic scale

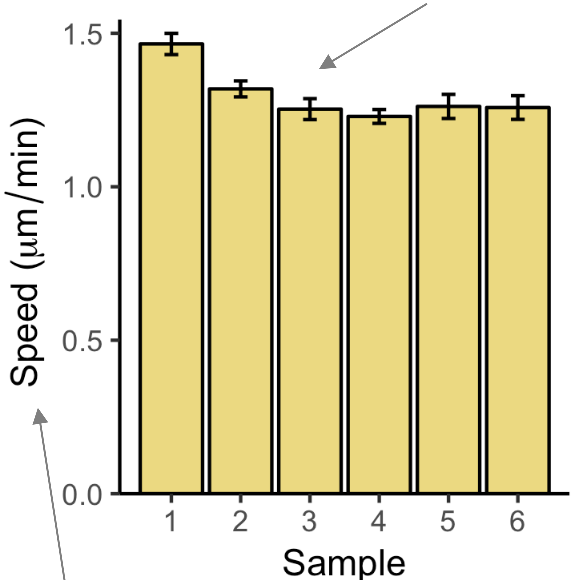


- There is no zero in a logarithmic scale!
- Bar size depends on an arbitrary lower limit of the vertical axis
- Don’t do it!

Bar plot problems

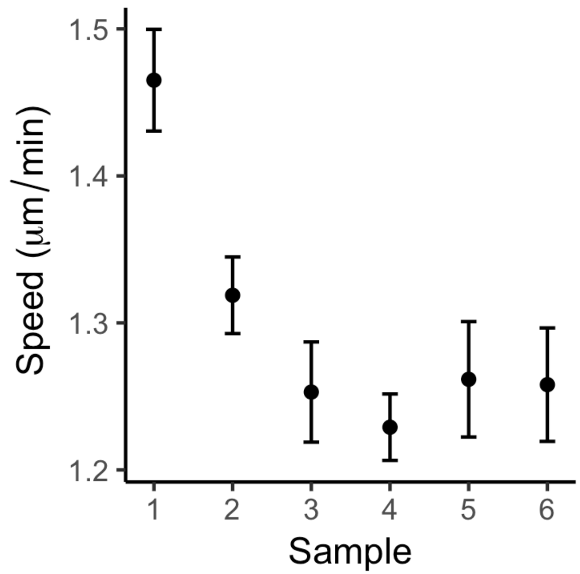
Bad

Little variability

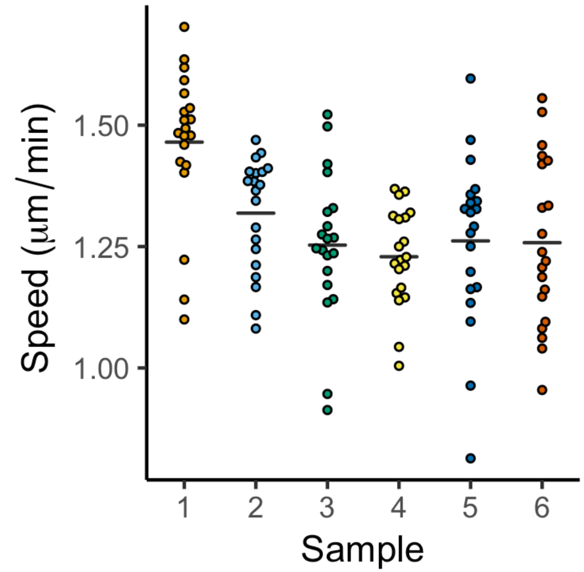


Not count based

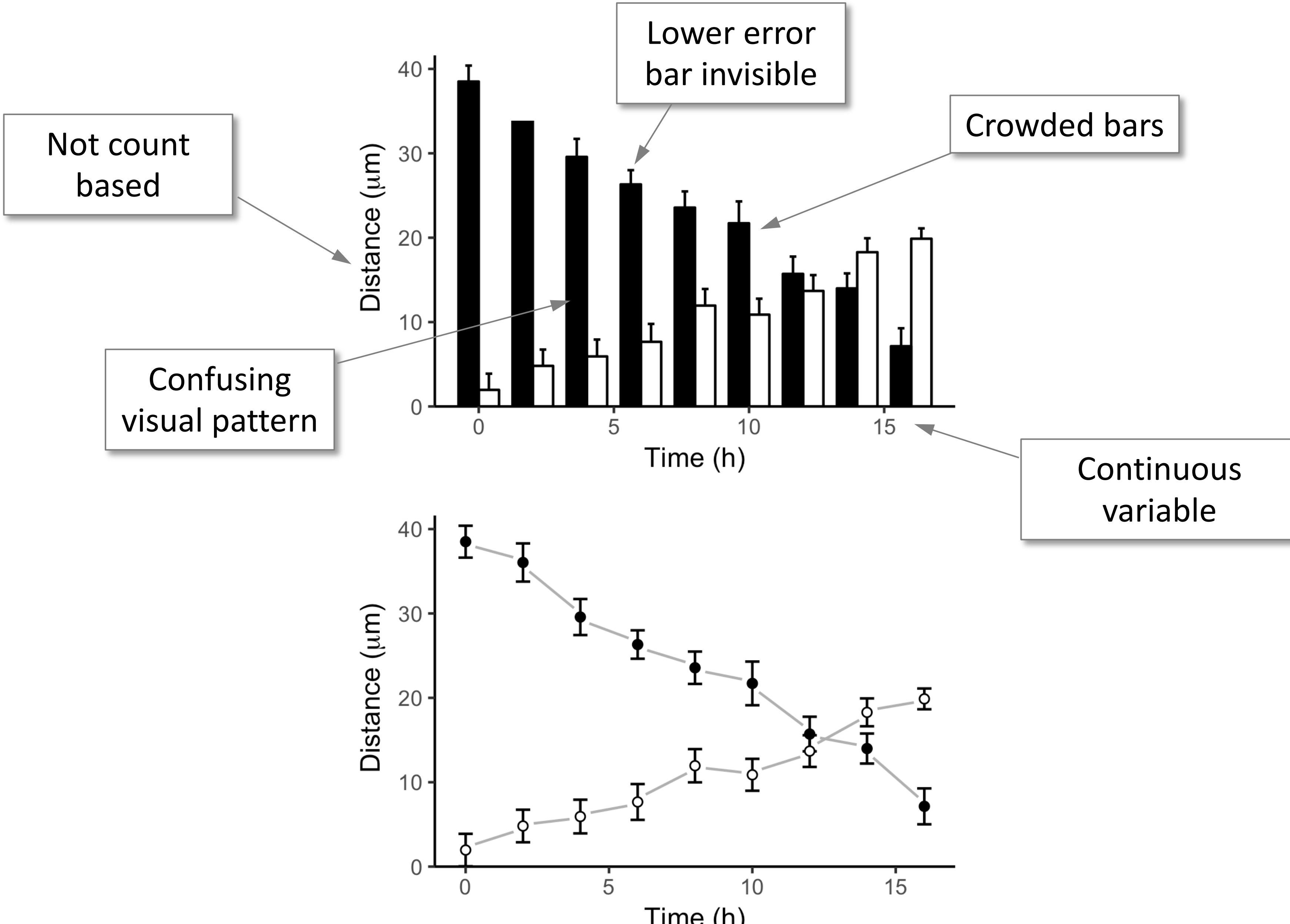
Better



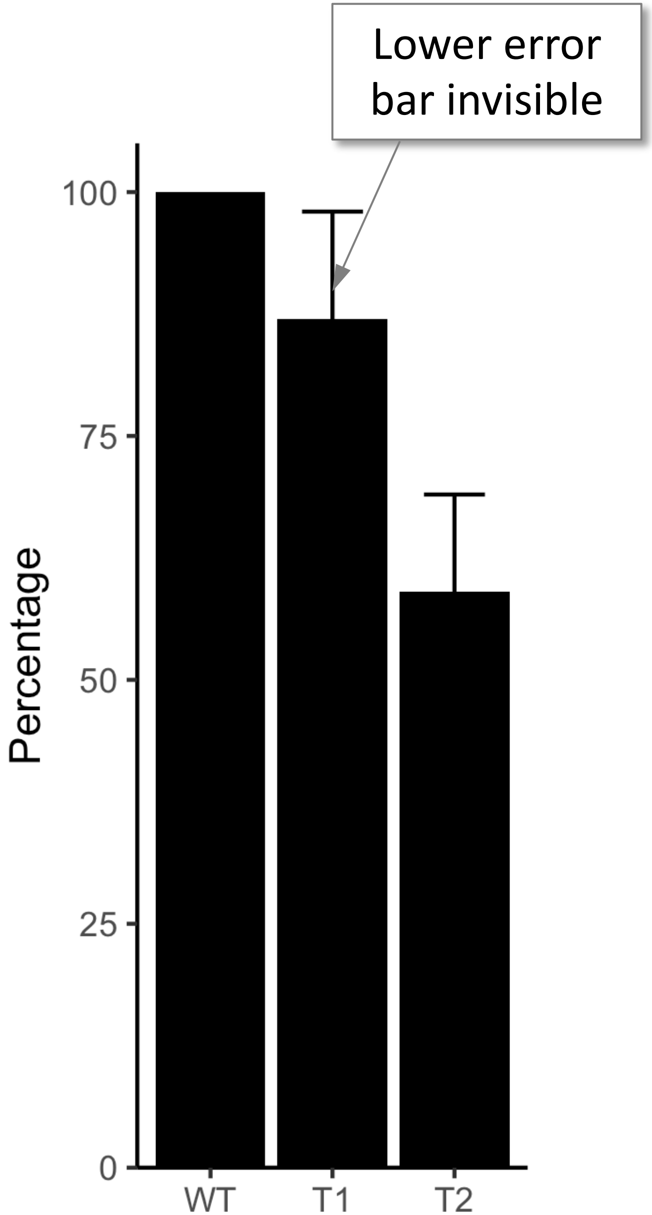
Best



Bar plot problems



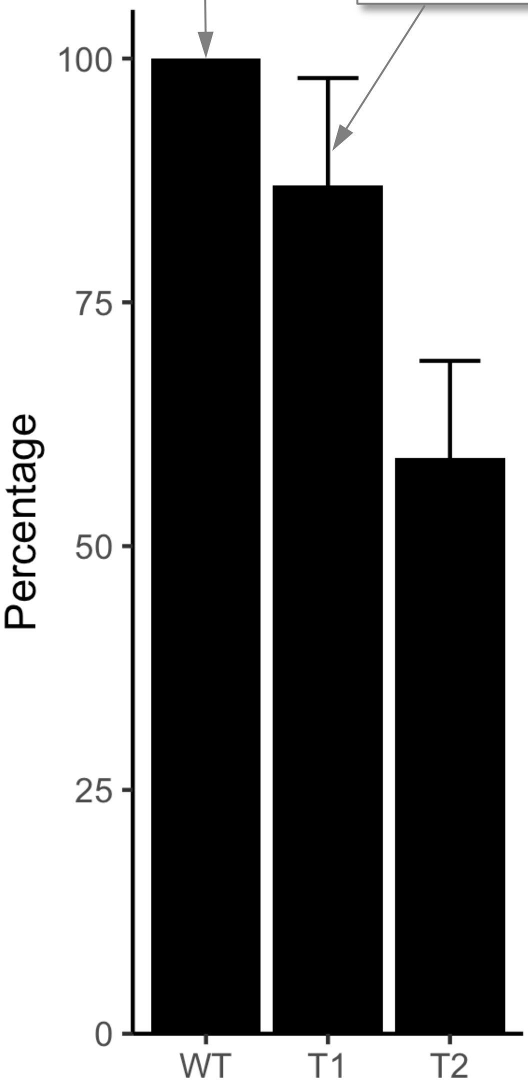
Bar plots with error bars



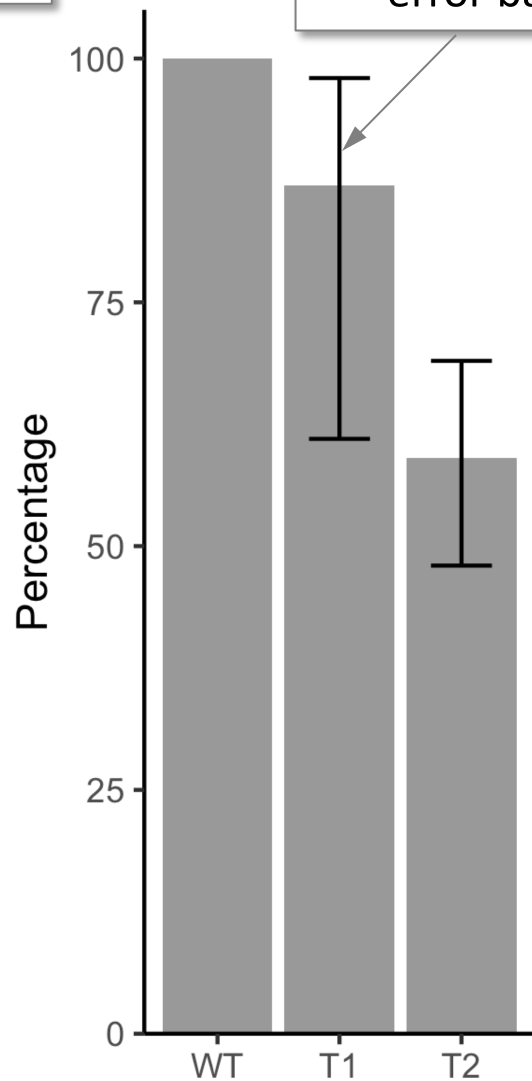
Bar plots with error bars

Useless information

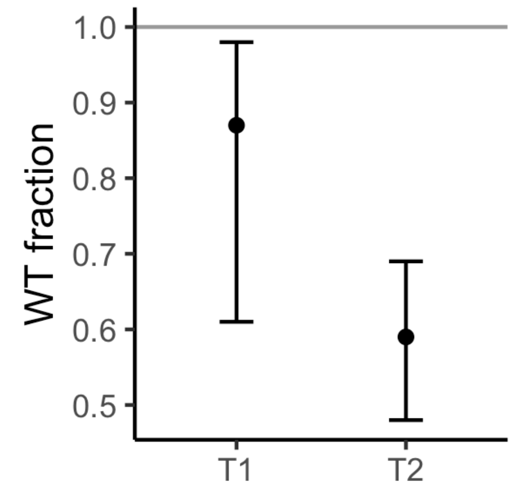
Lower error bar invisible



Always show upper and lower error bars



Other types of plots might be better

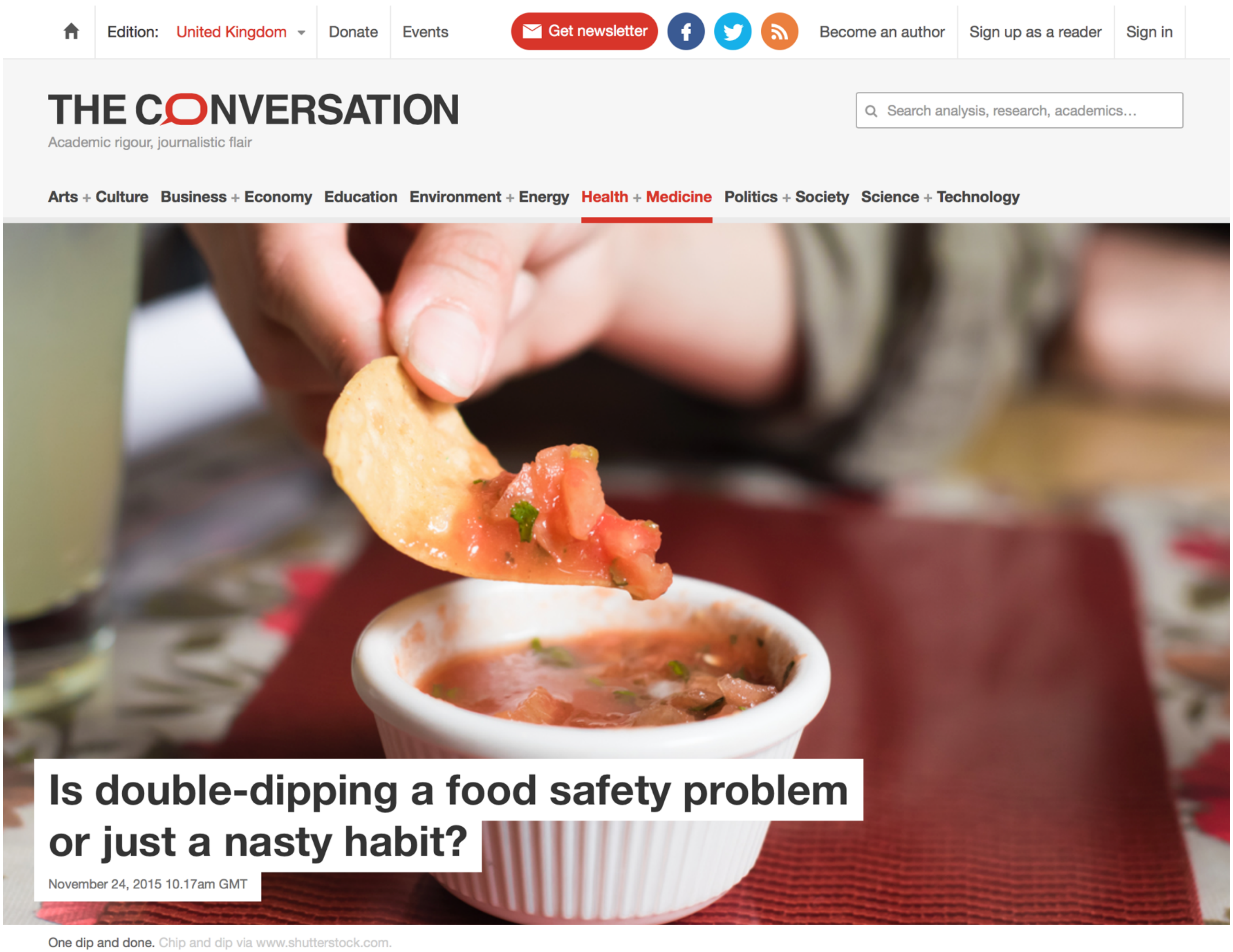


$T1 = 0.87^{+0.11}_{-0.26}$

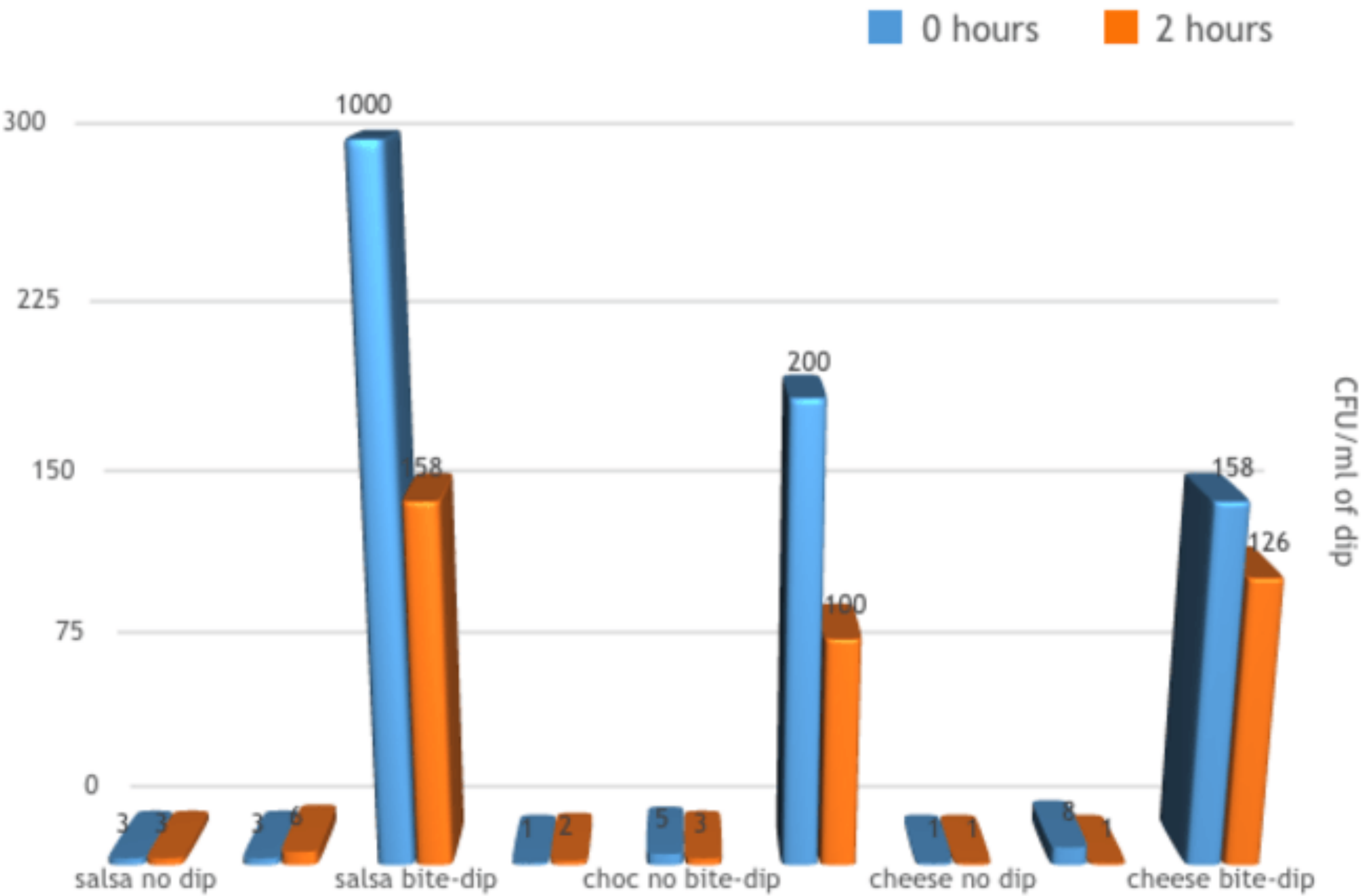
$T2 = 0.59^{+0.10}_{-0.11}$

Do you really need a plot?

The worst bar plot in the world?



The worst bar plot in the world?



Pie charts

NO

Rules of making good graphs

1. Always keep **clarity of presentation** in mind
2. You shall use axes with scales and labels
3. Use logarithmic scale to show data spanning over many orders of magnitude
4. All labels and numbers should be easy to read
5. Symbols shall be easy to distinguish
6. Add error bars where possible
7. Always state what type of uncertainty is represented by your error bars
8. Use model lines, where appropriate
9. It is OK to join data points with lines for guidance
10. You shall not use bar plots unless necessary

Bar plots: recommendations

1. Bar plots should only be used to present count-based quantities: counts, proportions and probabilities
2. Often it is to show whole data instead, e.g., a box plot or a histogram
3. Each bar has to start at zero
4. Don’t even think of making a bar plot in the logarithmic scale
5. Bar plots are not useful for presenting data with small variability
6. Multiple data bar plots are not suited for plots where the horizontal axis represents a continuous variable
7. Multiple data bar plots can be cluttered and unreadable
8. Make sure both upper and lower errors in a bar plot are clearly visible
9. You shall not make dynamite plots. Ever

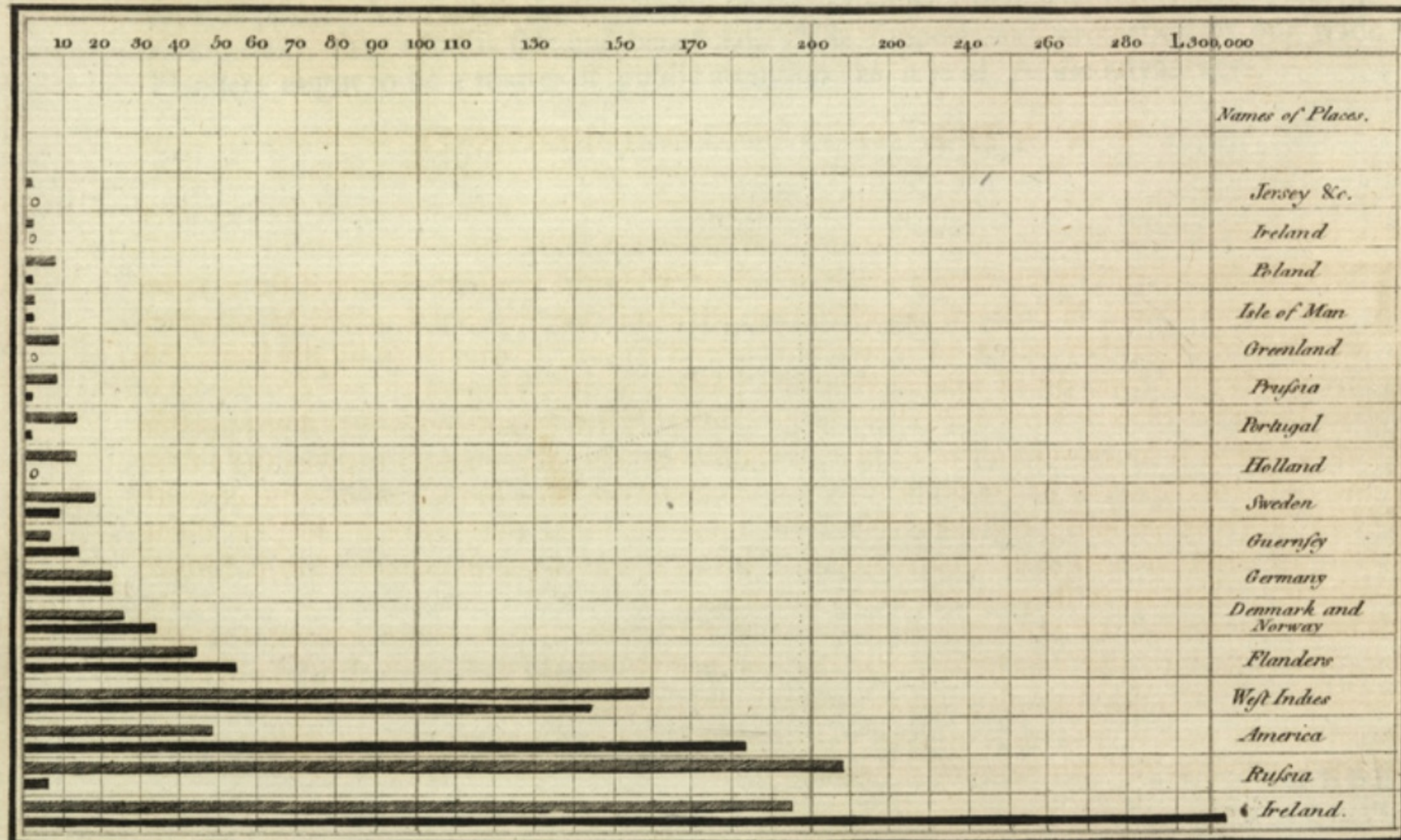
William Playfair

- Born in Liff near Dundee
- Man of many careers (millwright, engineer, draftsman, accountant, inventor, silversmith, merchant, secret agent, investment broker, economist, statistician, pamphleteer, translator, publicist, land speculator, blackmailer, swindler, convict, banker, editor and journalist)

- He invented
  - line graph (1786)
  - bar plot (1786)
  - pie chart (1801)

William Playfair (1759-1823)

Exports and Imports of SCOTLAND to and from different parts for one Year from Christmas 1780 to Christmas 1781.



The Upright divisions are Ten Thousand Pounds each. The Black Lines are Exports the Ribbed lines Imports.

6. Quoting numbers and errors

"23.230814584530889987945556640625%"

Anonymous

What is used to quantify errors

- In a publication you typically quote:

$$x = \underbrace{x_{\text{best}}}_{\text{best estimate}} \pm \underbrace{\Delta\text{x}}_{\text{error}}$$

- Error can be:
  - Standard deviation
  - Standard error of the mean
  - Confidence interval
  - Derived error
- Make sure you tell the reader what type of errors you use

Significant figures (digits)

- Significant figures (or digits) are those that carry meaningful information
- More s.f. – more information
- The rest is meaningless junk!
- Quote only significant digits

Example

- A microtubule has grown 4.1 μm in 2.6 minutes; what is the speed of growth of this microtubule?

$$\frac{4.1\ \mu\mathrm{m}}{2.6\ \mathrm{min}} = 1.576923077\ \mu\mathrm{m\ min}^{-1}$$

- There are only two significant figures (s.f.) in length and speed
- Therefore, only about two figures of the result are meaningful: 1.6 μm min^{-1}

Significant figures in writing

- Non-zero figures are significant
- Leading zeroes are not significant
  - 34, 0.34 and 0.00034 carry the same amount of information
- Watch out for trailing zeroes
  - before the decimal dot: not significant
  - after the decimal dot: significant

Number	Significant figures
365	3
1.893	4
4000	1 or 4
4$\times 10^3$	1
4.000$\times 10^3$	4
4000.00	6
0.000**34**	2
0.000**3400**	4

Rounding

- Remove non-significant figures by rounding
- Round the last s.f. according to the value of the next digit
  - 0-4: round down (**1.3**42 → 1.3)
  - 5-9: round up (**1.3**56 → 1.4)
- So, how many figures are significant?

Suppose we have 2 s.f. in each number

Raw number	Quote
1234	1200
1287	1300
1.491123	1.5
1.449999	1.4

Error in the error

- To find how many s.f. are in a number, you need to look at its error
- Use sampling distribution of the standard error
- Error in the error is

$$\Delta SE = \frac{SE}{\sqrt{2(n-1)}}$$

- This formula can be applied to SD and CI

Example

$n = 12$

$SE = 23.17345$

$$\Delta SE = \frac{23.17345}{\sqrt{2\times 11}} \approx \frac{23.17}{4.69} \approx 4.94$$

$SE = 23.17 \pm 4.94$

- We can trust only one figure in the error
- Round SE to one s.f.:

$SE = 20$

Error in the error

n	$\frac{\Delta SE}{SE}$	s.f. to quote
10	0.24	1
100	0.07	2
1,000	0.02	2
10,000	0.007	3
100,000	0.002	3

- An error quoted with 3 s.f. (2.567 ± 0.165) implicitly states you have 10,000 replicates

Quote number and error

- Get a number and its error
- Find how many significant figures you have in the error (typically 1 or 2)
- Quote the number with the *same decimal precision* as the error

Number	1.23457456	75156
Error	0.02377345	12223

Align at the decimal point

Round the last s.f. and reject insignificant figures

Round the last s.f. and replace insignificant figures with zeroes

Correct	Incorrect
1.23 ± 0.02	1.2 ± 0.02
1.2 ± 0.5	1.23423 ± 0.5
6.0 ± 3.0	6 ± 3.0
75000 ± 12000	75156 ± 12223
$(3.5 \pm 0.3)\times 10^{-5}$	$3.5 \pm 0.3\times 10^{-5}$

Error with no error

- Suppose you have a number without error
- (Go back to your lab and do more experiments)

- For example
  - Centromeres are transported by microtubules at an average speed of 1.5 μm/min
  - The new calibration method reduces error rates by ~5%
  - Transcription increases during the first 30 min
  - Cells were incubated at 22°C

- There is an **implicit error** in the last significant figure
- All quoted figures are presumed significant

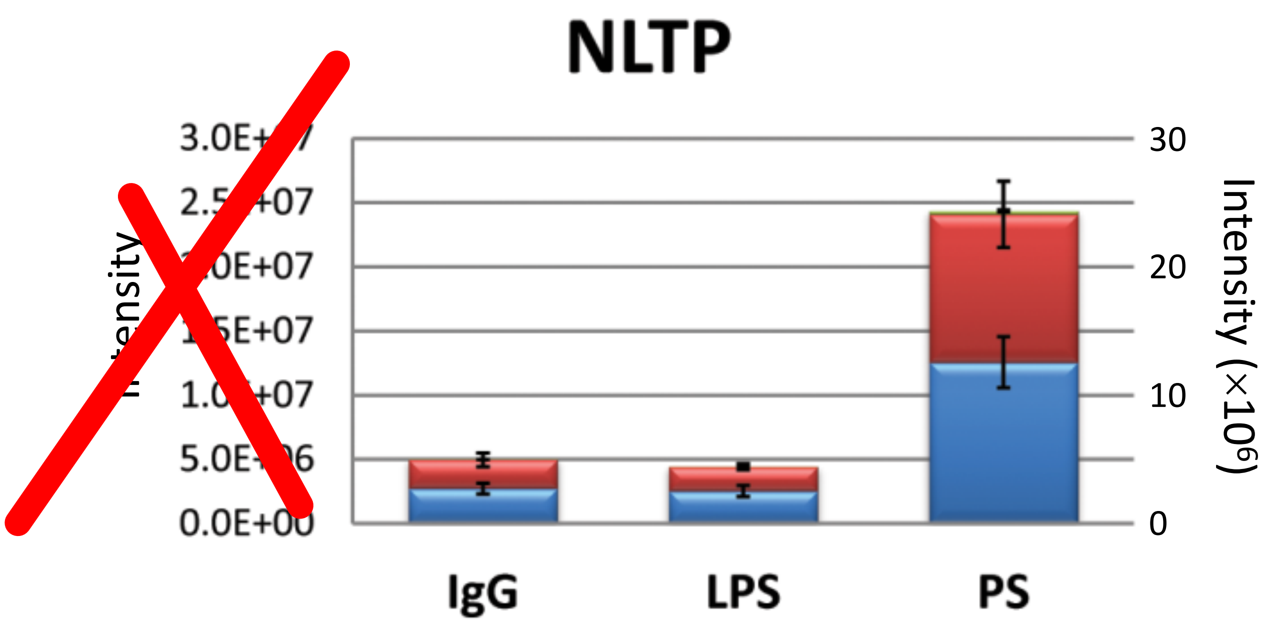
Avoid computer notation

- Example from a random paper off my shelf

  "p-value = 5.51E-14"

- I'd rather put it down as

  p-value = 6×10^{-14}



Fixed decimal places

- Another example, sometimes seen in papers
- Numbers with fixed decimal places, copied from *Excel*
- Typically fractional errors are similar and we have the same number of s.f.

raw data	1 decimal place
14524.21	14524.2
2234.242	2234.2
122.1948	122.2
12.60092	12.6
2.218293	2.2
0.120024	0.1
0.021746	0.0

Wrong	Right
14524.2	1.5×10^4
2234.2	2200
122.2	120
12.6	13
2.2	2.2
0.1	0.12
0.0	0.022

Assume there are only
2 s.f. in these measurements

How to quote numbers (and errors)

WHEN YOU KNOW ERROR

- First, calculate the error and estimate its uncertainty
- This will tell you how many significant figures of the error to quote
- Typically you quote 1-2 s.f. of the error
- Quote the number with **the same precision as the error**
  - 1.23 ± 0.02
  - 1.23423 ± 0.00005 (rather unlikely in biological experiments)
  - 6 ± 3
  - 75 ± 12
  - $(3.2 \pm 0.3)\times 10^{-5}$

WHEN YOU DON'T KNOW ERROR

- You still need to guesstimate your error!
- Quote only figures that are significant, e.g. $p = 0.03$, not $p = 0.0327365$
- Use common sense!
- Try estimating order of magnitude of your uncertainty
- Example: measure distance between two spots in a microscope
  - Get 416.23 nm from computer software
  - Resolution of the microscope is 100 nm
  - Quote 400 nm

Rounding numbers
0-4: down (6.64 → 6.6)
5-9: up (6.65 → 6.7)

Hand-outs available at
https://dag.compbio.dundee.ac.uk/training/Statistics_lectures.html